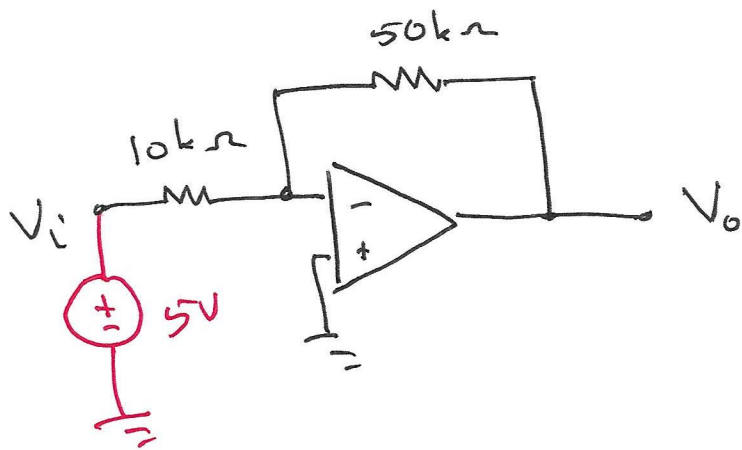


$$V_f = R_f \frac{V_s}{R_1}$$

$$-V_{out} - V_f + 0 = 0$$

$$V_{out} = -V_f = -\frac{R_f}{R_1} V_s$$

Amplifier with gain  
magnitude of  $\frac{R_f}{R_1}$

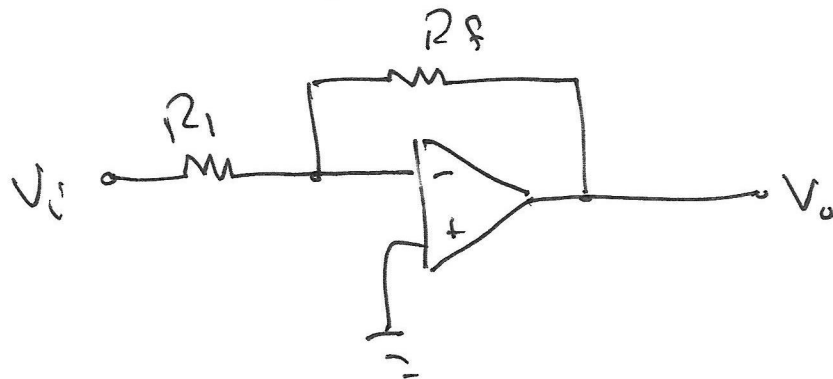


$$V_o = -\frac{50k\Omega}{10k\Omega} \cdot V_i$$

$$= -5 \cdot V_i$$

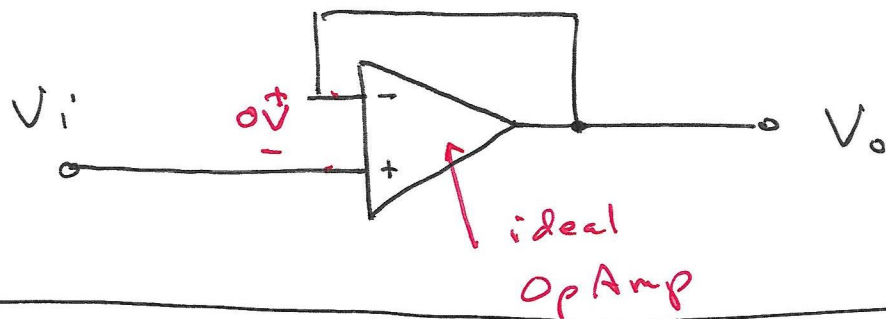
$$V_o = -5(5) = -25V$$

## Inverting Amplifier

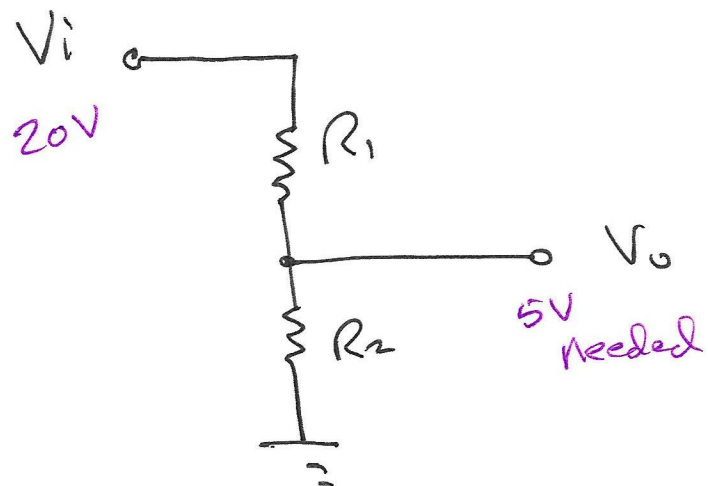


$$V_o = - \frac{R_f}{R_1} V_i$$

## Buffer



$$V_o = V_i$$

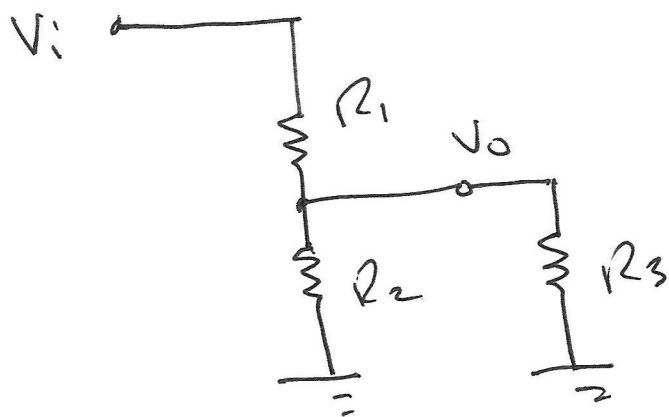


$$V_o = \frac{R_2}{R_1 + R_2} V_i$$

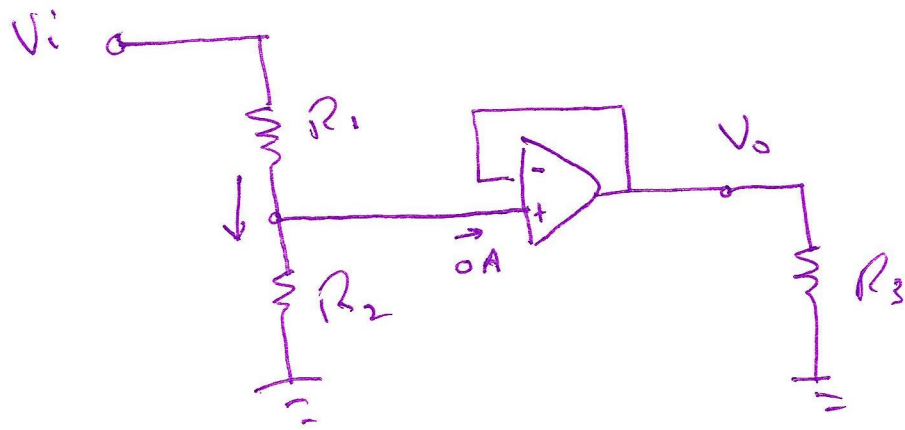
Choose  $R_1 = 3R_2$

$$V_o = \frac{1}{4} V_i$$

Connect a load.

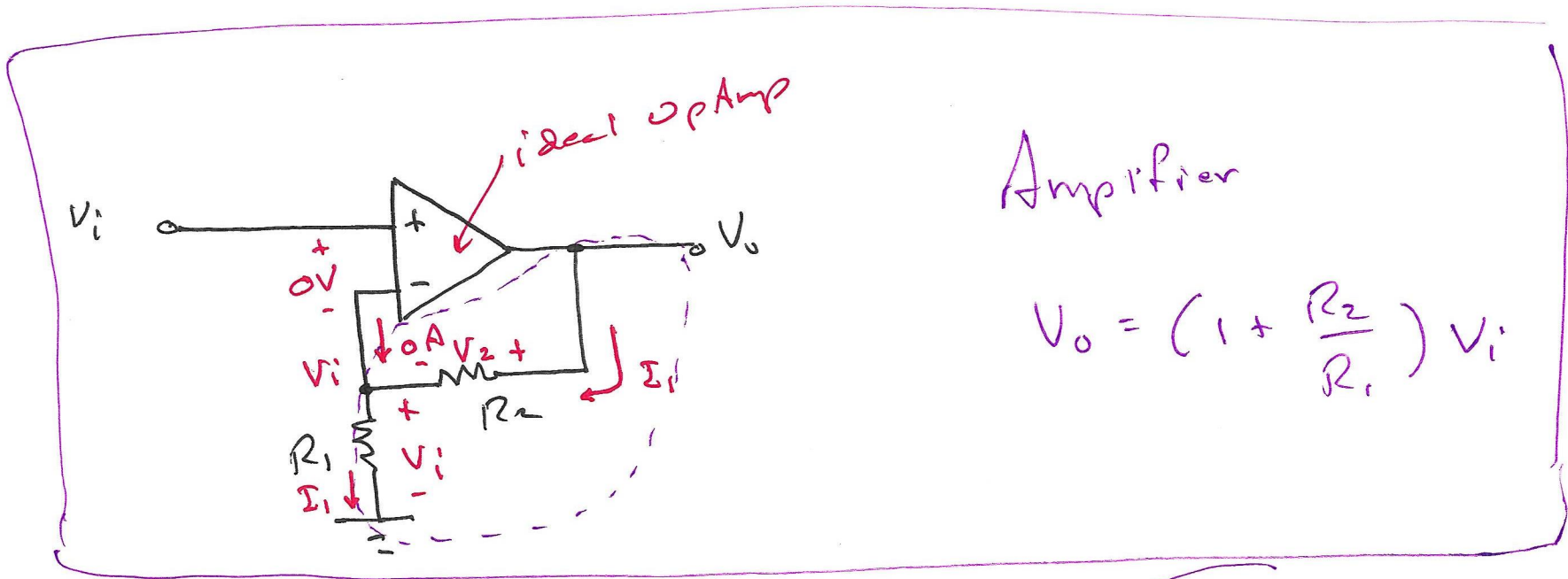


$$V_o = \frac{R_2 \parallel R_3}{R_1 + (R_2 \parallel R_3)} V_i$$



$$V_o = \frac{R_2}{R_1 + R_2} V_i$$

Because the buffer prevents current from flowing through  $R_3$  (i.e., prevents loading)

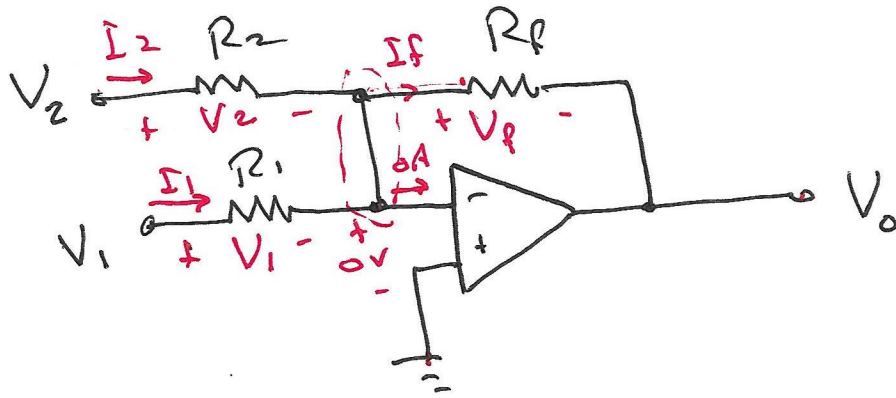


$$I_1 = \frac{V_i}{R_1}$$

$$V_2 = R_2 I_1 = R_2 \frac{V_i}{R_1}$$

$$-V_0 + V_2 + V_i = 0$$

$$V_0 = V_i + \frac{R_2}{R_1} V_i = \left(1 + \frac{R_2}{R_1}\right) V_i$$



$$I_1 = \frac{V_1}{R_1}$$

$$I_2 = \frac{V_2}{R_2}$$

Summing Amplifier

$$I_f = I_1 + I_2$$

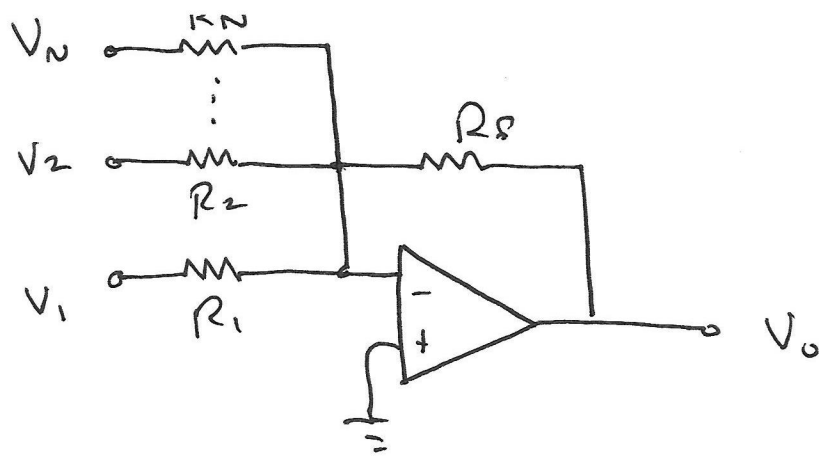
$$= \frac{V_1}{R_1} + \frac{V_2}{R_2}$$

$$V_p = R_f I_f$$

$$= \frac{R_f}{R_1} V_1 + \frac{R_f}{R_2} V_2$$

$$V_0 = -V_p$$

$$V_0 = -\frac{R_f}{R_1} V_1 - \frac{R_f}{R_2} V_2$$



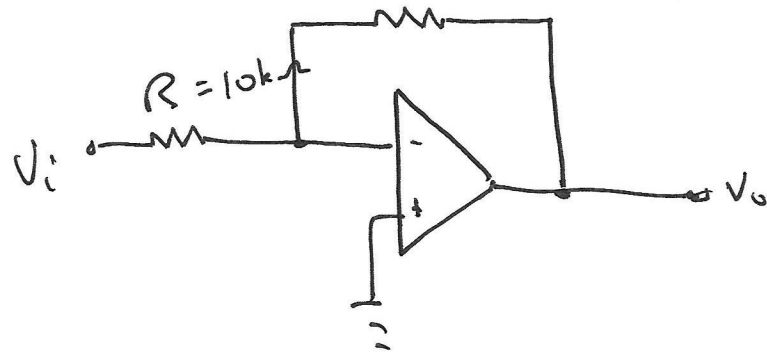
Summing Amplifier

$$V_o = - \frac{R_f}{R_1} V_1 - \frac{R_f}{R_2} V_2$$

$$- \dots - \frac{R_f}{R_N} V_N$$

Design a circuit that converts  $-5V$  to  $+7V$ .

$$\frac{7}{5}R = 14k\Omega$$



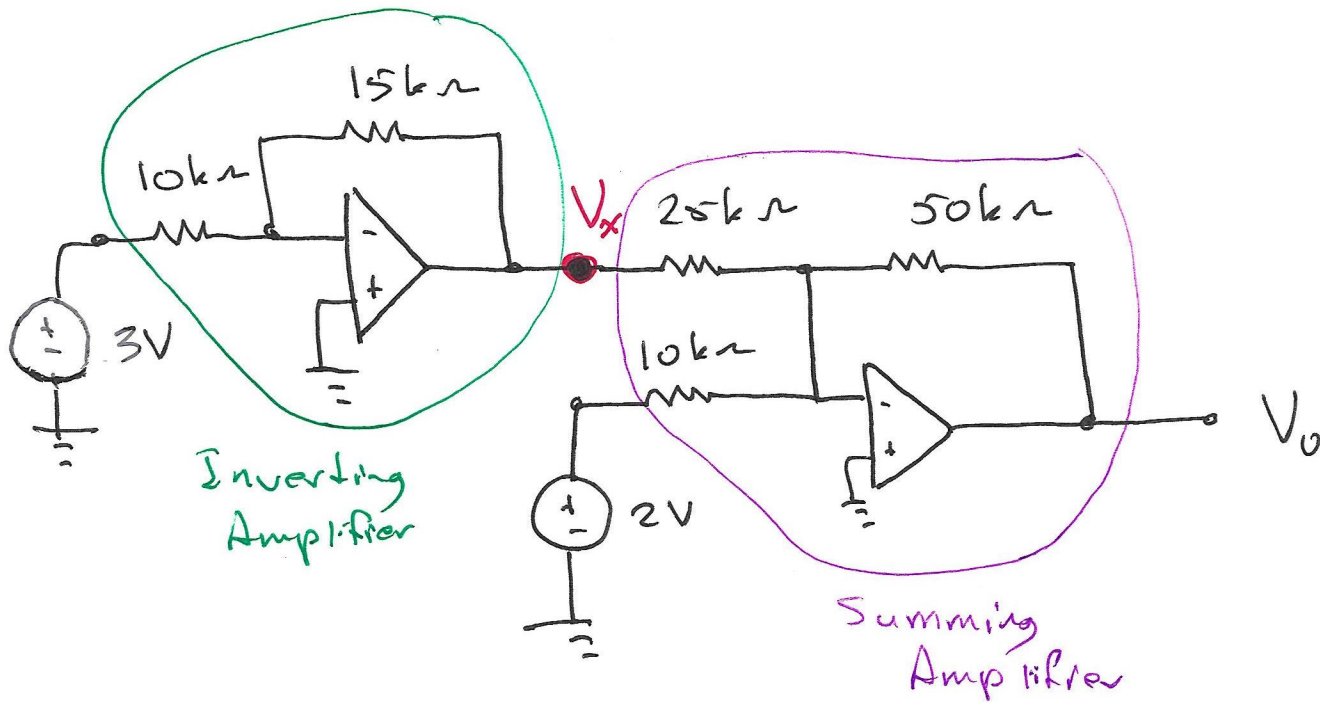
Choose  $R = 10k\Omega$

Then  $\frac{7}{5}R = 14k\Omega$

$$V_o = - \frac{14k\Omega}{10k\Omega} V_i = -1.4 V_i$$

$$\text{for } V_{in} = 5V, \quad V_o = -1.4(5) = -7V$$





$$V_x = - \frac{15k\Omega}{10k\Omega} 3V = - \frac{9}{2} V = -4.5V$$

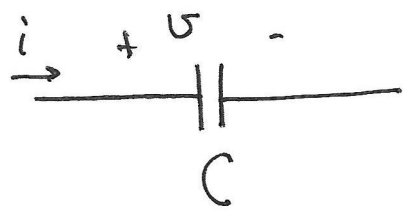
$$V_o = - \frac{50k\Omega}{25k\Omega} V_x - \frac{50k\Omega}{10k\Omega} (2V)$$

$$= -2(-4.5) - 5(2)$$

$$= 9 - 10$$

$$= -1 V$$

# Capacitor



units of capacitance are Farads (F).

If  $v$  and  $i$  satisfy the PSC, then

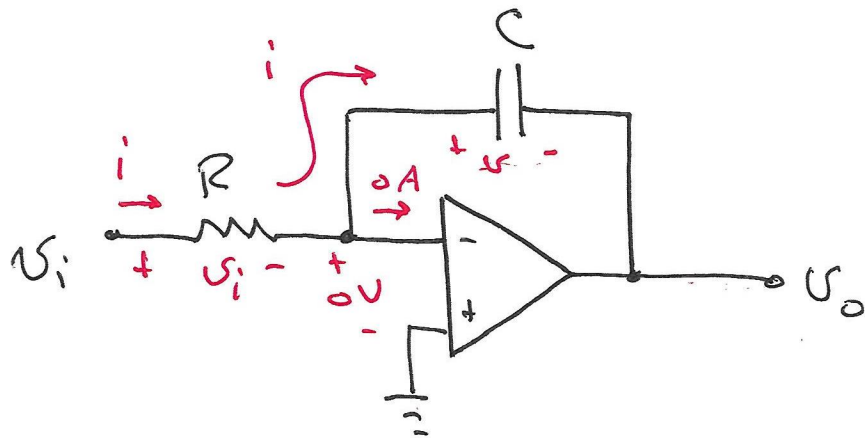
$$i = C \frac{dv}{dt}$$

$$Q = Cv$$

$$\frac{dQ}{dt} = C \frac{dv}{dt}$$

current

$$v = v_0 + \frac{1}{C} \int_0^t i dt$$



$$i = \frac{U_i}{R}$$

$$U = U_{\text{initial}} + \frac{1}{C} \int_0^t i \, dt$$

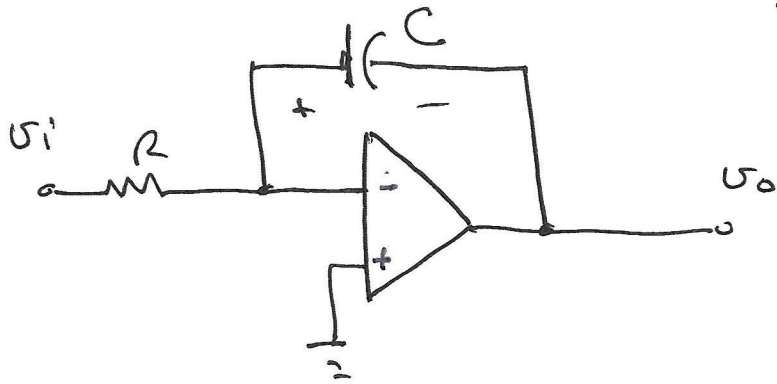
$$U = U_{\text{initial}} + \frac{1}{Rc} \int_0^t U_i \, dt$$

If the capacitor is not initially charged:

$$U = \frac{1}{Rc} \int_0^t U_i \, dt$$

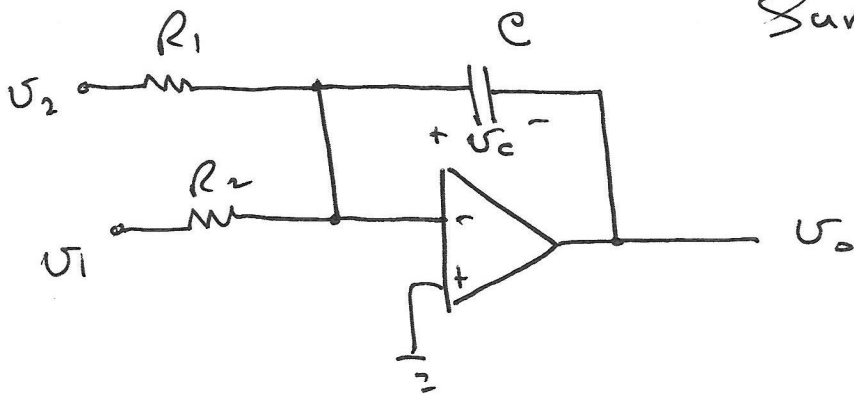
$$\Rightarrow U_o = - \frac{1}{Rc} \int_0^t U_i \, dt$$

## Integrator

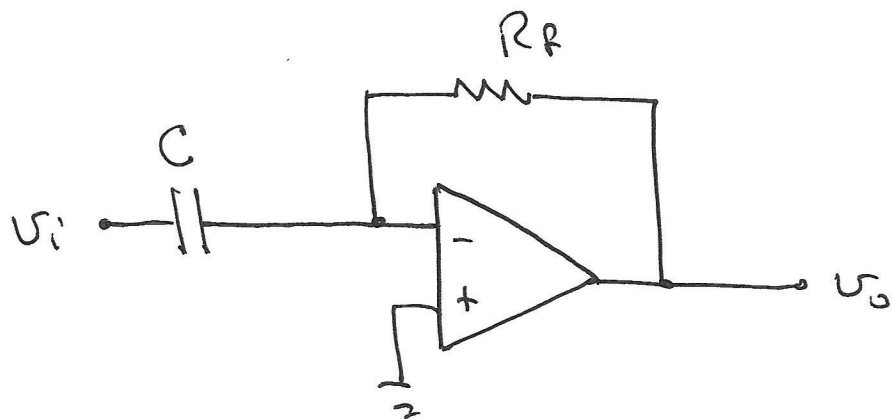


$$v_o = v_{\text{initial}} - \frac{1}{Rc} \int_0^t v_i dt$$

## Summing Integrator



$$v_o = v_c(0) - \frac{1}{R_2 c} \int_0^t v_1 dt - \frac{1}{R_1 c} \int_0^t v_2 dt$$



How is  $u_o$  related to  $u_i$ ?

(For next time.)